

# Ch 6 Rational functions

① Domain

$$g(x) = \frac{x-4}{x-6}$$

$$\{x \mid x \in \mathbb{R}, \text{ but } x \neq 6\}$$

$\mathbb{R} \setminus \{6\}$

Things you  
can't do in  
math

①  $\div$  by zero

$$\frac{15}{12} = \frac{\cancel{3} \cdot 5}{2 \cdot 2 \cdot \cancel{3}} = \frac{5}{4}$$

find the domain

$$f(x) = \frac{x-4}{x^2-16} = \frac{x-4}{(\cancel{x-4})(x+4)} = \frac{1}{x+4}$$

$$\{x \mid x \in \mathbb{R}, x \neq -4, 4\}$$

$$\frac{7-5}{5-7} = \frac{2}{-2} = -1 \quad \frac{x+3}{x-3}$$

$$\frac{\begin{array}{r} -1 \\ +x-3 \end{array}}{\cancel{3-x}} = \frac{\cancel{x-3}}{-(\cancel{x-3})} = -1$$



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$$\frac{a^3 - a^2 - 8a + 8}{a^2 - 4} = \frac{(a^2 - 4)(a + 2) + 2a + 4}{(a-2)(a+2)}$$

$$\frac{a^2 + 2a + 4}{a^2 + 2a + 4}$$

$$\frac{a^2 + 2a + 4}{a + 2}$$

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$$\frac{m^2(m^2 - 4) + 6(m - 4)}{m^2(m^2 - 4)}$$

$$\frac{(m-4)(m+4) + 6(m-4)}{(m-4)(m+4)}$$

$$\frac{(m^2 + 6)(m-4)}{(m-4)(m+4)} = \frac{m^2 + 6}{m+4}$$

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$$\frac{(x+3)(x-2)}{(x+3)}$$

$$= \frac{(x+3)(x-2)}{(x+3)}$$

$$= x-2$$

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$$\frac{(9+6)(9-7)}{(9-2)(9-7)}$$

$$\frac{(9+6)(9-7)}{(9-2)(9-7)}$$

$$\frac{9+6}{9-2}$$

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$$\frac{(y-10)(y+2)}{(10+y)(10-y)}$$

$$= \frac{100 - y^2}{100 - y^2}$$

$$\frac{y+2}{y+10}$$

$$\frac{-y-2}{y+10}$$

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$$\frac{(x+2)(x-2)}{(x+2)(x-2)}$$

$$= 1$$

$$-x+2$$

$$-x+$$

$$\frac{x^2 - 4}{-2 - x} \rightarrow \frac{\cancel{(x+2)}(x-2)}{-\cancel{(x+2)}}$$

"

$$-(x-2) = -x+2$$